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An Improved Biometric Multi-Server Authentication Scheme for Chang et al.'s Protocol

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The remote authentication has been advancing with the growth of online services being offered on remote basis. This calls for an optimal authentication framework other than single-server authentication. In this connection, the multi-server authentication architecture has been introduced in the literature that enables the users to avail variety of services of various service providers, using a single pair of identity and password. Lately, we have witnessed a few multi-server authentication protocols in the literature that had several limitations. One of those multi-server authentication protocols has been put forward by Chang et al. recently. Our analysis shows that the Chang et al.'s scheme is susceptible to impersonation threat, stolen smart card threat. In this study, we have reviewed the protocol thoroughly, and proposed an improved model, that is resistant to all known and identified threats. The formal security analysis along with discussion of informal analysis for contributed model is also presented in this study, besides performance and its evaluation analysis.

KEYWORDS: Multiserver authentication, cryptanalysis, biometrics, remote authentication, attacks.

1. Introduction

The growth of internet has facilitated the day-to-day introduction of new services on remote basis. In this regard, an efficient Multi-Server Authentication (MSA) serves as an integral component of this growth, which lets the users avail remote services from different servers, by utilizing a single pair of identity and password for all servers [10, 21, 29, 33]. MSA not only relieves the user of the hassle of memorizing so many passwords, but also relaxes the servers of individualized registration procedures with each user, prior to the authentication phase [17]. In the last five years, many multi-server authentication schemes were presented. Nevertheless, there is still a need of more secure and efficient techniques [35]. In MSA literature, for neural networks, Li et al. [23], Lin et al. [30], Juang [18], Chang and Lee [3] contributed few techniques that were based on symmetric cryptography and discrete logarithms. However, these schemes did not protect the identity of user, and were also computationally inefficient for their operations cost. Afterwards, Liao and Wang [28] presented a dynamic identity-based MSA protocol. However, the scheme was found vulnerable by Hsiang and Shih [9], for lacking mutual authentication, and improved scheme was presented by Hsiang and Shih. Then, Yeh et al. [36] found that the previous scheme is exposed to session key disclosure, replay threat, and forgery threat. Thereafter, Lee et al. [22] indicated that Yeh et al.'s scheme is prone to masquerading attack and also lacks mutual authentication. At the same time, Sood et al. [34] specifies that the same Yeh et al. protocol suffers stolen smart card, impersonation threat, and a flawed password changing procedure. Sood et al. and Lee et al. also demonstrated their enhanced

models. Then, Li et al. [24, 27] discovered a mutual authentication weakness in Sood et al. protocol, and server spoofing, faulty authentication procedure in Lee et al.'s scheme [22], with contribution of improved schemes, respectively. Afterwards, Chang et al. [5] proposed a dynamic identity based authentication scheme, which was found to be vulnerable in impersonation threat, stolen smart card threat, insider threat, and password-guessing threat by Li et al. [26]. The Li et al. [24] protocol was found to be vulnerable against forgery attack by Chang et al. [4] and an inherent design weakness was discovered by Chang et al. that was providing the attacker a chance to perform illegal activities without being caught. Thereafter, Chang et al. put forward an enhanced model for protocol [24]. After careful study of Chang et al. [4], we found that the Chang et al.'s model is prone to impersonation threat, and session key disclosure attacks, once smart card gets stolen. We have contributed an enhanced biometric authentication model that covers all of the indicated limitations in the Chang et al. scheme. This study work demonstrates formal analysis of security and performance evaluation as well.

Our protocol is arranged in the following order: The section "Preliminaries" defines the preliminaries related to our scheme and section "A review of the Chang et al.'s protocol" presents a review and cryptanalysis of Chang et al.'s protocol. The section "Proposed model" demonstrates our contributed protocol. The section "Security discussion" and section "Formal security analysis" illustrate informal and formal security analysis, respectively. The "Comparison and performance analysis" section depicts the related performance analysis. The last section summarizes this paper.

2. Preliminaries

The properties of hash digest and bio-hashing function are illustrated in preliminaries section.

2.1. Hash Function

To act as a secure authentication protocol, one of the constituent lightweight crypto-operations, i.e. a one-way hash function $h: \{0, 1\}^* \rightarrow Z_q^*$, must hold the under-stated features.

- 1 The function h generates a fixed length hash digest after taking a variable sized input.
- 2 In case $h(\mu)=\delta$, it is hard in polynomial time for computing $h^{-1}(\delta)=\mu$;
- 3 If μ is given, it is improbable to compute μ' in polynomial time, such that $\mu' \neq \mu$ holds as well as $h(\mu') = h(\mu)$;
- 4 In addition, it is hard to get a pair (μ, μ') given that $\mu' \neq \mu$ and $h(\mu')=h(\mu)$ holds at the same time.

2.2. Bio-hashing

The bio-hashing function [19] is employed for capturing the inherent biometric features of a person, such as fingerprint to be used for authentication purpose, while these features remains permanent over a period of time. Jin et al. [16], in 2004 came up with a two-factor authenticator protocol which bears iterated inner products, as kept between tokenized pseudorandom number and user-oriented finger impression-based features. This procedure computes a particular compact code which provides the basis for the current bio-hashing concept. Thereafter, this bio-hashing function was improved further by Lumini and Loris [32]. The bio-hashing function produces a unique random vector as a function of specific user's biometric features, which is named as a Biocode. This, in addition, helps in discretizing the projection-coefficients and is computed as secure hashed password in general.

3. A Review of the Chang et al.'s Scheme

The protocol's working of Chang et al. [4] is described as under.

3.1. Revisiting Chang et al.'s Model

The Chang et al.'s model [4] is comprised of three procedures, such as the registration procedure, mutual authentication procedure which is also shown in Figure 1. We present a few notations that may be helpful to readers to comprehend the scheme as given in Table 1.

Table 1

Symbols guide

| Notations | Meaning |
|--------------|--|
| U_i : | i^{th} Subscriber or User |
| IDI, PW_i | Subscriber's identity and password |
| $H()$: | Private hash function |
| $H_B()$: | Bio-hashing function |
| SP_j : | The j^{th} service provider |
| RC : | Registration centre |
| $h(\cdot)$: | a secure hash digest function |
| Bi : | Biometric impression |
| K, b : | RC's master secret, RC's random secret |
| n_i, n_j : | Nonce |
| SC : | Smart Card |
| $\ , \oplus$ | Concatenation and XOR functions |

3.1.1. Server Registration Procedure

The Chang et al.'s model comprises a reliable registration centre (**RC**) along with n number of servers (**SP_j**), while the range of j implies $1 \leq j \leq n$. The **SP_j** completes its registration procedure with RC before the user's registration. The **SP_j** is registered from **RC** with the sharing of two secrets K_1 and K_2 between **SP_j** and **RC** over a confidential channel. Earlier, RC selects a master secret key k and a random integer b . Afterwards, **SP_j** submits the identity **SID_j** towards registration centre. Then, RC calculates $K_1 = h(k \| b)$ and $K_2 = h(\text{SID}_j \| H(b))$. Here, $H(\cdot)$ is a private hash digest, while $h(\cdot)$ represents public hash-digest function. Onwards, the registration centre forwards these keys to **SP_j** employing a confidential channel.

Figure 1

Chang et al.'s registration and mutual authentication procedure

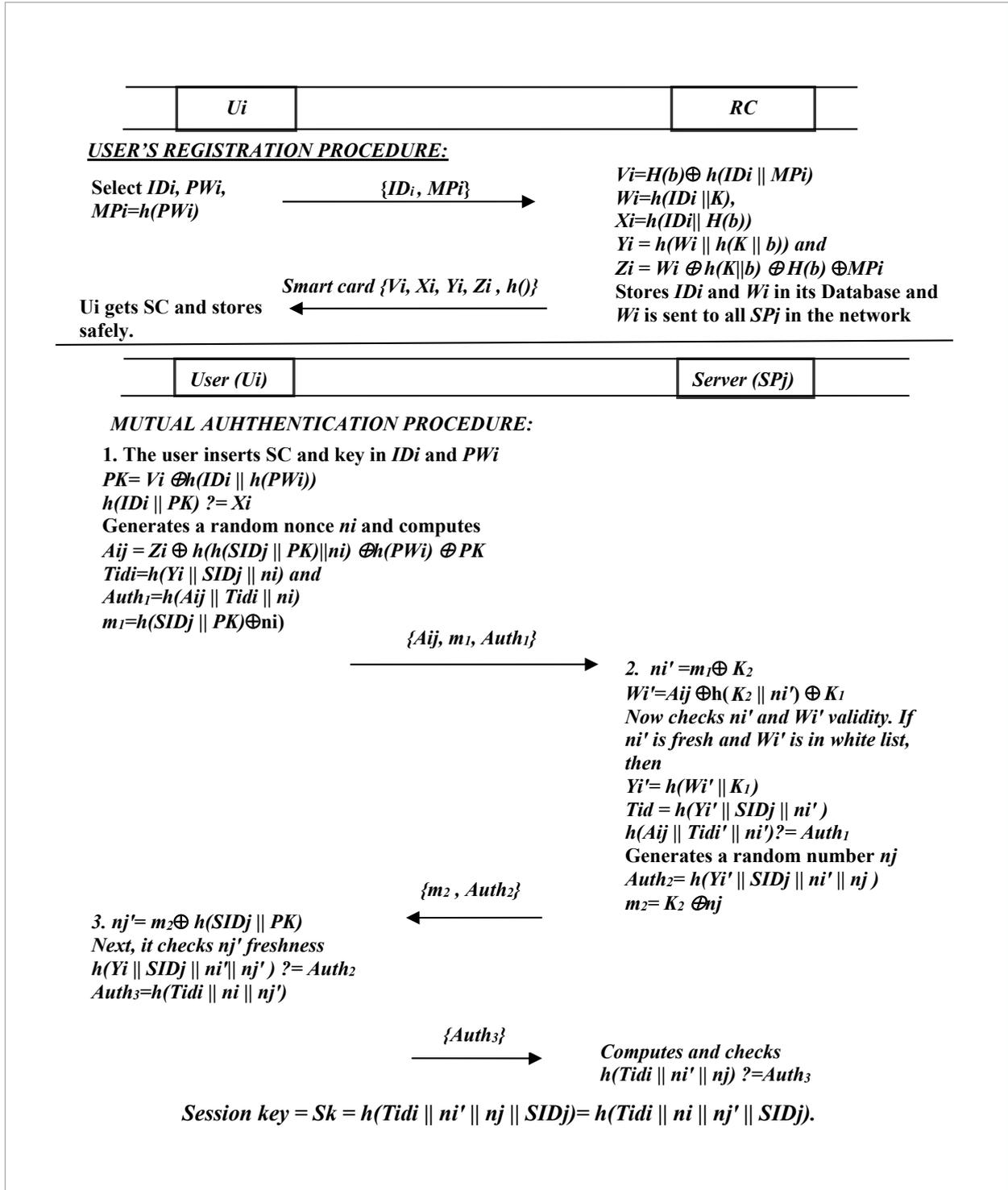
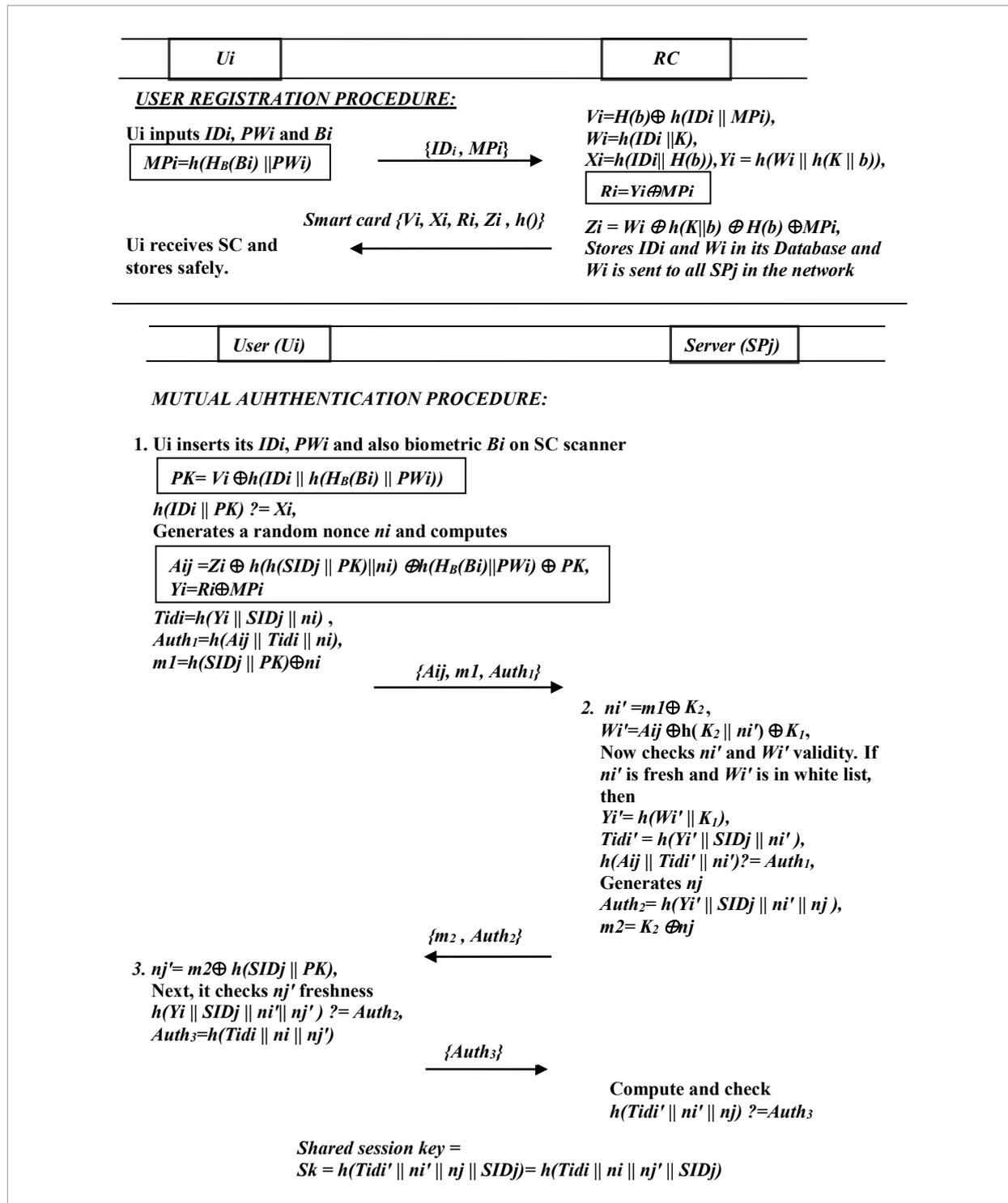


Figure 2

Proposed model



3.1.2. User Registration Procedure

In the registration procedure, U_i performs few registration steps with the RC. Afterwards U_i may access all service providers SP_j . The RC performs the under-mentioned steps with the user to implement the registration procedure.

- 1 Primarily, U_i chooses its identity (ID_i) and a password (PW_i). Then, it computes MP_i by calculating $MP_i = h(PW_i)$ and it sends $\{ID_i, MP_i\}$ to SP_j as shown in Figure 1.
- 2 SP_j , then, calculates $V_i = H(b) \oplus h(ID_i || MP_i)$, $W_i = h(ID_i || k)$, $X_i = h(ID_i || H(b))$, $Y_i = h(W_i || h(k || b))$ and $Z_i = W_i \oplus h(k || b) \oplus H(b) \oplus MP_i$. Afterwards, SP_j stores ID_i and W_i in its database, while W_i is sent to all servers in the network. RC now issues smart card to U_i with these parameters $\{V_i, X_i, Y_i, Z_i$ and $h(b)\}$.

3.1.3. Mutual Authentication Procedure

- 1 In this procedure, U_i employs its smart card to avail the SP_j 's services. For this reason, the user inserts SC and gives ID_i and PW_i as input. Next, it computes $PK = V_i \oplus h(ID_i || h(PW_i))$ and checks the equality $h(ID_i || PK) \stackrel{?}{=} X_i$. On successful check, it produces a random nonce ni and calculate $A_{ij} = Z_i \oplus h(h(SID_j || PK) || ni) \oplus h(PW_i) \oplus PK$, $Tidi = h(Y_i || SID_j || ni)$, $Auth_1 = h(A_{ij} || Tidi || ni)$ and $m_2 = h(SID_j || PK) \oplus ni$. Next, it submits the message $\{A_{ij}, m_2, Auth_1\}$ to SP_j for verification.
- 2 The SP_j receives $\{A_{ij}, m_2, Auth_1\}$ and computes $ni' = m_2 \oplus K_2$ and $Wi' = A_{ij} \oplus h(K_2 || ni') \oplus K_1$. SP_j now checks validity and freshness of ni' and Wi' . If ni' is fresh and Wi' is in its white list, it computes $Yi' = h(Wi' || K_1)$ and $Tidi' = h(Yi' || SID_j || ni')$. Next, it checks the equality $h(A_{ij} || Tidi' || ni') \stackrel{?}{=} Auth_1$. If true, it engenders a random integer n_j and further calculates $Auth_2 = h(Yi' || SID_j || ni' || n_j)$, $m_2 = K_2 \oplus n_j$. Next, it sends $\{m_2, Auth_2\}$ to U_i .
- 3 After receiving $\{m_2, Auth_2\}$, U_i calculates $n_j' = m_2 \oplus h(SID_j || PK)$. He/She checks the validity or freshness for n_j' and computes $h(Yi || SID_j || ni' || n_j')$ for checking the validity $h(Yi || SID_j || ni' || n_j') \stackrel{?}{=} Auth_2$. If true, then calculates $Auth_3 = h(Tidi || ni || n_j')$, and sends the message $\{Auth_3\}$ to SP_j as acknowledgement.
- 4 SP_j receives $Auth_3$ message and computes $h(Tidi || ni' || n_j')$ for checking $h(Tidi || ni' || n_j') \stackrel{?}{=} Auth_3$.

If it proves to be valid, a session key is computed between the participants, as $Sk = h(Tidi || ni' || n_j' || SID_j) = h(Tidi || ni || n_j' || SID_j)$.

3.2. Cryptanalysis of Chang et al.'s Protocol

The Chang et al.'s protocol is a multi-server authentication-based scheme relying on simple hash and XOR operations. Before presenting the limitations in Chang et al.'s model, we assume that adversary is proficient in the following capabilities.

- The adversary may intercept, modify or manipulate the message contents communicated on insecure public channel.
- The adversary may access the smart card and its parameters by stealth.
- The adversary might not get any of the contents communicated on secure channel, for instance, in registration phase.

The Chang et al.'s protocol is susceptible to the following attacks.

3.2.1. Impersonation Attack

The Chang et al.'s protocol is prone to impersonation attack if the user's smart card contents are revealed to adversary. Suppose, Eve, a valid but malicious user happens to steal the user's smart card contents in some manner. In this context, Eve seize all SC parameters $\{V_i, X_i, Y_i, Z_i\}$ and intercepts public messages $\{A_{ij}, m_2, Auth_1, m_2, Auth_2, Auth_3\}$. Next, Eve may adopt the following steps to launch an impersonation attack.

- 1 Initially, Eve computes PK such as $PK = V_i \oplus h(ID_{Eve} || MP_i)$, where PK and $H(b)$ represent the same parameters.
- 2 Then, Eve computes $ni = h(SID_j || PK) \oplus m_2$.
- 3 Next, the PW_i , being a low entropy password, can easily be guessed by applying and testing various combinations PW_i^* in the equation $A_{ij} \stackrel{?}{=} Z_i \oplus h(h(SID_j || PK) || ni) \oplus h(PW_i^*) \oplus PK$. Wherever the match is found, the valid PW_i becomes known.
- 4 After the seizure of SC contents and guessing the password PW_i , Eve may launch impersonation attacks on both sides (user and server). *On user's end*, having the knowledge of Y_i and Z_i , Eve generates a nonce ni and constructs the login message $\{A_{ij}, m_2, Auth_1\}$ comfortably by computing

$Tidi=h(Yi \parallel SIDj \parallel ni)$, $Auth_1=h(Aij \parallel Tidi \parallel ni)$, and $m_2=h(SIDj \parallel PK) \oplus ni$ towards server. On server's end, while impersonating as a server, Eve sends the message $\{m_2, Auth_2\}$ towards user by generating fresh nonce nj and computing $Auth_2=h(Yi \parallel SIDj \parallel ni' \parallel nj)$ and $m_2=h(SIDj \parallel PK) \oplus nj$.

3.2.2. No Session Key Security

In Chang et al.'s protocol, the attacker could deduce the session key comfortably, once the smart card is accessed by it. Since the session key is composed as $Sk=h(Tidi \parallel ni \parallel nj \parallel SIDj)$, Eve may try to reproduce Sk on the basis of computed elements. For this purpose, Eve, having the knowledge of $\{Vi, Xi, Yi, Zi, m_2\}$ parameters, computes $PK=Vi \oplus h(ID_{Eve} \parallel MPi)$, $ni=h(SIDj \parallel PK) \oplus m_2$, $nj=h(SIDj \parallel PK) \oplus m_2$, and $Tidi=h(Yi \parallel SIDj \parallel ni)$. Finally, Eve can generate the session key by concatenating as $Sk=h(Tidi \parallel ni \parallel nj \parallel SIDj)$. In this manner, Eve may generate all previous session keys by approaching the publicly available messages as communicated between the legal participants.

4. Proposed Scheme

Our proposed model is based on countering the limitations in Chang et al.'s model. The contributed model comprises service provider (server's) registration procedure, user's registration procedure, mutual authentication procedure, and password upgrading procedure.

4.1. Server Registration Procedure

The proposed model comprises a trustworthy RC and n number of servers (SPj), while the range of j implies $1 \leq j \leq n$. The SPj performs the registration with RC prior to user's registration procedure, using a secret channel. During initialization process, RC selects a master secret key k , and also chooses a random secret b . Then, SPj forwards its identity SIDj towards registration centre. Next, RC computes the two keys as $K_1=h(k \parallel b)$ and $K_2=h(SIDj \parallel H(b))$, and sends both keys (K_1 and K_2) to SPj employing a confidential channel. In this manner, the SPj gets registered through RC.

4.2. User Registration Procedure

In registration phase, Ui registers with registration centre (RC) and follows the under-mentioned steps:

- 1 The user initially selects its identity as IDi , password as PWi , and the biometric as Bi [17]. Subsequently, Ui calculates $MPi=h(H_B(Bi) \parallel PWi)$ and submits $\{IDi, MPi\}$ to SPj.
- 2 Next, SPj calculates $Vi=H(b) \oplus h(IDi \parallel MPi)$, $Wi=h(IDi \parallel k)$, $Xi=h(IDi \parallel H(b))$, $Yi=h(Wi \parallel h(k \parallel b))$, $Ri=Yi \oplus MPi$, and $Zi=Wi \oplus h(k \parallel b) \oplus H(b) \oplus MPi$, and stores IDi and Wi in its database, while Wi is sent to all SPj in the network. Next, RC issues smart card to Ui with these parameters $\{Vi, Xi, Ri, Zi$ and $hO\}$.

4.3. Mutual Authentication Procedure

In this stage, the user is mutually authenticated with server SPj and uses smart card to avail services. The related procedure is shown in Figure 2.

- 1 Initially, Ui inserts its smart card in scanner and also inputs its ID and PWi . Then, it captures the biometric imprint Bi . Afterwards, Ui calculates $PK=Vi \oplus h(IDi \parallel h(H_B(Bi) \parallel PWi))$ and verifies the equality for $h(IDi \parallel PK) \stackrel{?}{=} Xi$. If true, then Ui engenders a random integer ni and further calculates $Aij=Zi \oplus h(h(SIDj \parallel PK) \parallel ni) \oplus h(H_B(Bi) \parallel PWi) \oplus PK$, $Yi=Ri \oplus MPi$, $Tidi=h(Yi \parallel SIDj \parallel ni)$, $Auth_1=h(Aij \parallel Tidi \parallel ni)$ and $m_2=h(SIDj \parallel PK) \oplus ni$. Then, Ui sends the message $\{Aij, m_2, Auth_1\}$ to SPj for verification.
- 2 Next, the SPj receives the message $\{Aij, m_2, Auth_1\}$ and computes $ni'=m_2 \oplus K_2$ and $Wi'=Aij \oplus h(K_2 \parallel ni') \oplus K_1$. The SPj confirms the validity and freshness of ni' and Wi' . If ni' is fresh and Wi' is in the white list, then it further computes $Yi'=h(Wi' \parallel K_1)$ and $Tidi'=h(Yi' \parallel SIDj \parallel ni')$. Now, it verifies the equation $h(Aij \parallel Tidi' \parallel ni') \stackrel{?}{=} Auth_1$. If this proves to be true, it engenders a random number nj , and computes $Auth_2=h(Yi' \parallel SIDj \parallel ni' \parallel nj)$ and $m2=K_2 \oplus nj$. Then, it sends $\{m_2, Auth_2\}$ to Ui for further verifications.
- 3 Upon receiving $\{m_2, Auth_2\}$ from SPj , Ui calculates $nj'=m_2 \oplus h(SIDj \parallel PK)$. Ui checks the validity for nj' and computes $h(Yi \parallel SIDj \parallel ni' \parallel nj')$ for verifying the validity for $h(Yi \parallel SIDj \parallel ni' \parallel nj') \stackrel{?}{=} Auth_2$. If this equation is found to be valid, it calculates $Auth_3=h(Tidi \parallel ni \parallel nj')$, and sends the message $\{Auth_3\}$ to SPj as an acknowledgement finally.
- 4 Upon having the message $Auth_3$, the SPj calculates $h(Tidi \parallel ni' \parallel nj)$ for verifying $h(Tidi \parallel ni' \parallel nj)$

$?=Auth_3$. If true, then develops the ultimate session key as $Sk = h(Tidi || ni' || nj || SIDj) = h(Tidi || ni || nj' || SIDj)$.

4.4. Password Updating Procedure

Ui modifies his/her old password (PWi) with a fresh password (PWi^{fr}) without involving RC, by adopting the under-mentioned steps:

- 1 To modify the password, the user would input his/her identity as IDI , old password as PWi into the smart card. Next, the user imprints biometric identity Bi into a device scanner.
- 2 Subsequently, SC computes $PK = Vi \oplus h(IDi || h(H_B(Bi) || PWi))$ and validates the equality $h(IDi || PK) ?= Xi$. If it does not match, the smart card aborts the session, otherwise allows the user to proceed on the next step.
- 3 After that, the user would insert a new password as PWi^{fr} in SC, which calculates $Vi^{new} = PK \oplus h(IDi || h(H_B(Bi) || PWi^{fr}))$, $Ri^{new} = Ri \oplus h(H_B(Bi) || PWi) \oplus h(H_B(Bi) || PWi^{fr})$, and $Zi^{new} = Zi \oplus h(H_B(Bi) || PWi) \oplus h(H_B(Bi) || PWi^{fr})$. Then, the user replaces the Vi , Ri and Zi parameters in smart card with the new values Vi^{new} , Ri^{new} and Zi^{new} .

5. Security Discussion

This segment illustrates the informal security discussion for contributed model in comparison with Chang et al.'s model.

5.1. Replay Attacks

These attacks may be attempted by an attacker after replaying the seized message contents at opportune time to deceive any legal entity of the protocol.

An attacker A could seize the communication contents after examining a public channel as $\{Aij, m_2, Auth_p, m_2, Auth_2, Auth_3\}$ and attempt to replay at some opportune time in future towards a valid participant. Nonetheless, A cannot construct the parameter $Auth_p$, as it also comprises Aij which includes Ei and $h(H_B(Bi) || PWi)$ in its construction, such as $Aij = Zi \oplus h(h(SIDj || PK) || ni) \oplus h(H_B(Bi) || PWi) \oplus PK$. An attacker A neither knows the password nor biometric Bi , which prevents the attacker for launching the replay attack. If A replays the message $\{Aij, m_2, Auth_3\}$

to SPj , it may not be able to construct the upgraded challenge $Auth_3$, which requires the computation of $Tidi$, which further needs Yi to be constructed that is inaccessible to A even if the SC gets stolen. At the same time, if A replays the message $\{m_2, Auth_2\}$ towards Ui , the latter may easily detect the attack, since Ui knows that $Auth_2$ cannot be constructed by the adversary due to the non-availability of Yi parameter. Hence, our proposed protocol may counter any replay threat.

5.2. Man-In-The-Middle-Attack

In this threat, the attacker intrudes between the legal participants by acting as an intermediary through replaying or modifying the message contents. A successful attack may let the legitimate members communicate with the adversary perceiving it as a right participant [6].

An adversary cannot construct the message $\{Auth_2, m_2\}$ in request of $\{Aij, m_2, Auth_3\}$, since the construction of $Auth_2$ requires Yi , which is inaccessible to A from either intercepted messages or SC contents. Then, A constructs a valid $Auth_3$ against SPj 's challenge $\{Auth_2, m_2\}$, as $Tidi$ is inaccessible to A due to unknown Yi . Therefore, the contributed scheme is protected from MiTM threat.

5.3. Modification Threats

Such threats could be initiated by an attacker if it transforms the communication message illegally for submitting it to any valid participant [19].

An adversary may attempt to construct the message $\{Aij, m_2, Auth_3\}$, however it may not be able to do so, since it needs the parameter Aij , that further requires the knowledge of PWi and Bi as $Aij = Zi \oplus h(h(SIDj || PK) || ni) \oplus h(H_B(Bi) || PWi) \oplus PK$. Likewise, it requires $Tidi$ to construct $Auth_p$, which requires the knowledge of Yi , which is also inaccessible to A due to the unreachable MPI . Similarly, an adversary is not able to construct the message $\{Auth_2, m_2\}$ in request of $\{Aij, m_2, Auth_3\}$, given that the production of $Auth_2$ requires the information of Yi , which is not accessible to A either from intercepted messages or stolen SC contents.

5.4. Password or Secret Guessing Threat

An attacker A might try to recover password PWi either from messages intercepted or from stolen smart card contents. The password guessing requires the attacker

to be familiar with biometric information \mathbf{Bi} of the user. If \mathbf{Bi} is not available, then the password \mathbf{PWi} may not be inferred or guessed from \mathbf{Vi} , \mathbf{Zi} and \mathbf{Ri} parameters.

5.5. Session Key Disclosure Using Stolen Card

An attacker \mathcal{A} might steal smart card contents and try to generate a session key (\mathbf{Sk}) from its contents. Nonetheless, \mathcal{A} *cannot* calculate the session key $\mathbf{Sk} = h(\mathbf{Tidi} || \mathbf{ni} || \mathbf{nj} || \mathbf{SIDj})$ due to the inaccessible \mathbf{Tidi} parameter in \mathbf{Sk} . While, the \mathbf{Tidi} is constructed as $\mathbf{Tidi} = h(\mathbf{Yi} || \mathbf{SIDj} || \mathbf{ni})$ and the attacker cannot guess \mathbf{Yi} either from stolen card contents or intercepted messages.

5.6. Impersonation Attack Using Smart Card Contents

An attacker \mathcal{A} might steal smart card and try to impersonate the legitimate users or service provider by constructing the identical message $\{\mathbf{Aij}, \mathbf{m}_2, \mathbf{Auth}_2\}$. Nonetheless, it may not be able to do so [24], since it needs the parameter \mathbf{Aij} . Which further requires \mathbf{PWi} and \mathbf{Bi} to be guessed, as $\mathbf{Aij} = \mathbf{Zi} \oplus h(h(\mathbf{SIDj} || \mathbf{PK}) || \mathbf{ni}) \oplus h(H_B(\mathbf{Bi}) || \mathbf{PWi}) \oplus \mathbf{PK}$. Besides, it needs \mathbf{Tidi} to build \mathbf{Auth}_2 , which requires the value \mathbf{Yi} , which is also inaccessible to \mathcal{A} due to the unknown \mathbf{MPi} . Similarly, an adversary cannot construct the message $\{\mathbf{Auth}_2, \mathbf{m}_2\}$ in response to a valid user request $\{\mathbf{Aij}, \mathbf{m}_2, \mathbf{Auth}_2\}$, since, the construction of \mathbf{Auth}_2 requires the information of \mathbf{Yi} , which is not accessible to \mathcal{A} either from intercepted messages or stolen SC contents.

5.7. Session Key Security

This trait makes certain that the established session key is merely known to lawful members of a session, i.e. client and service provider.

In proposed model, the agreed session key, i.e. $\mathbf{Sk} = h(\mathbf{Tidi} || \mathbf{ni} || \mathbf{nj} || \mathbf{SIDj})$ is secure, since, the \mathbf{Tidi} calculation requires the access of \mathbf{Yi} , i.e., $\mathbf{Tidi} = h(\mathbf{Yi} || \mathbf{SIDj} || \mathbf{ni})$, while \mathbf{Yi} requires the value \mathbf{MPi} for guessing it, as $\mathbf{Yi} = \mathbf{Ri} \oplus \mathbf{MPi}$. Hence, the session key \mathbf{Sk} has been safe, in case the SC contents are accessed or \mathcal{A} intercepts the public parameters.

5.8. Known Key Security

This attribute makes certain the protection of private keys of participants in case the current session key is exposed.

In contributed protocol, even if the adversary accesses the values \mathbf{Sk} , \mathbf{Ri} , an attacker cannot recover user password \mathbf{PWi} , since the \mathbf{PWi} recovery from $\mathbf{Sk} = h(\mathbf{Tidi} || \mathbf{ni} || \mathbf{nj} || \mathbf{SIDj})$ requires calculation of $\mathbf{Yi} = \mathbf{Ri} \oplus \mathbf{MPi}$ and $\mathbf{Tidi} = h(\mathbf{Yi} || \mathbf{SIDj} || \mathbf{ni})$. This is not possible due to the inaccessibility of \mathbf{Bi} in $\mathbf{MPi} = h(H_B(\mathbf{Bi}) || \mathbf{PWi})$. At the same time, the server secret \mathbf{K} is also secure as it is existent in a function i.e $h(\mathbf{K} || \mathbf{b})$ and is hard be guessed in polynomial amount of time. Therefore, the proposed protocol keeps the feature of known key security.

5.9. Mutual Authentication

This attribute assures that the concerned members authenticate one another in the protocol session and construct a mutual session key ultimately [7].

In our scheme, both of the participants authenticate each other mutually on account of \mathbf{Tidi} and \mathbf{Yi} parameters. The server authenticates the user only if \mathbf{Tidi} is valid in \mathbf{Auth}_3 , and this \mathbf{Tidi} cannot be constructed by an attacker. Similarly, \mathbf{Ui} authenticates \mathbf{SPj} on account \mathbf{Yi} parameter used by server in the construction of $\mathbf{Auth}_2 = h(\mathbf{Yi} || \mathbf{SIDj} || \mathbf{ni} || \mathbf{nj})$. The \mathbf{Yi} parameter cannot be accessed by an attacker even through \mathbf{Ri} if the card gets stolen. Therefore, our protocol assures mutual authentication feature to the legitimate participants.

5.10. Anonymous Protocol

In an anonymous protocol [11, 12, 15], a legal user interacts with service provider without exposing its identity and an adversary may not recover the user's identity or secret credentials from intercepted contents on public channel.

In proposed scheme, the adversary cannot extract \mathbf{Ui} 's identity or other secret credentials out of intercepted contents on public channel or stolen smart card contents. This is because of the fact that the identity \mathbf{Idi} is protected in a secret function $\mathbf{Wi} = h(\mathbf{Idi} || \mathbf{K})$, which is not possible to guess until the server secret \mathbf{K} is exposed. Therefore, the contributed scheme confers anonymity to the user.

6. Formal Security Analysis

In this section, we exhibit the security strength of our protocol using formal analysis based on Burrows Aba-

di Needham-logic (BAN) [2] and random oracle model-based analysis.

The BAN logic proves the authenticated key agreement based on key distribution and mutual key agreement, and protocol robustness against the revelation of session key. We utilized few notations in this BAN logic proof as follows:

The agents interacting in a protocol are termed as *principals*

The symmetric encryption is performed using *keys* in a protocol.

Nonces in the protocol assist to distinguish various sessions.

We employed the following notations in proving the authenticity of our protocol using BAN logic:

$\beta \models \mathcal{Q}$: The principal β believes \mathcal{Q} ,

$\beta \triangleleft \mathcal{Q}$: β sees \mathcal{Q} .

$\beta \vdash \mathcal{Q}$: β once said \mathcal{Q} .

$\beta \Rightarrow \mathcal{Q}$: β has got jurisdiction over \mathcal{Q} .

$\#(\mathcal{Q})$: The message \mathcal{Q} is fresh.

$(\mathcal{Q}, \mathcal{Q}')$: \mathcal{Q} or \mathcal{Q}' are parts of message $(\mathcal{Q}, \mathcal{Q}')$.

$\langle \mathcal{Q} \rangle_{\mathcal{Q}'}$: The message \mathcal{Q} is combined with \mathcal{Q}' .

$\{\mathcal{Q}, \mathcal{Q}'\}_k$: \mathcal{Q} or \mathcal{Q}' is encrypted using key k .

$(\mathcal{Q}, \mathcal{Q}')_k$: \mathcal{Q} or \mathcal{Q}' is hashed with k .

$\mathcal{Q} \xrightarrow{k} \mathcal{Q}'$: \mathcal{Q} and \mathcal{Q}' exchange message employing the shared key k .

Some related postulates utilized in BAN logic are shown below:

$$P_r \text{ Message meaning postulate} \approx \frac{\beta \models \beta \xrightarrow{k} \beta', \beta \triangleleft (\mathcal{Q})_{\mathcal{Q}'}}{\beta \models \beta' \vdash \mathcal{Q}}$$

$$P_{\mathcal{Q}} \text{ Nonce verification postulate} \approx \frac{\beta \models (\mathcal{Q}), \beta \models \beta' \vdash \mathcal{Q}}{\beta \models \beta' \models \mathcal{Q}}$$

$$P_{\mathcal{Q}'} \text{ Jurisdiction postulate} \approx \frac{\beta \models \beta' \Rightarrow \mathcal{Q}, \beta \models \beta' \models \mathcal{Q}}{\beta \models \mathcal{Q}}$$

$$P_{\mathcal{Q}''} \text{ Freshness conjucatenation postulate} \approx \frac{\beta \models (\mathcal{Q}), \beta \models (\mathcal{Q}'')}{\beta \models (\mathcal{Q}, \mathcal{Q}'')}$$

$$P_{\mathcal{Q}'''} \text{ Belief postulate} \approx \frac{\beta \models (\mathcal{Q}), \beta \models (\mathcal{Q}''')}{\beta \models (\mathcal{Q}, \mathcal{Q}''')}$$

$$P_{\mathcal{Q}''''} \text{ Session keys postulate} \approx \frac{\beta \models (\mathcal{Q}), \beta \models \beta' \models \mathcal{Q}'}{\beta \models \beta \xrightarrow{k} \beta'}$$

The contributed scheme must meet the under-mentioned goals to prove its session key's security under BAN logic on the basis of above postulates:

$$\text{Goal-1: } S_r \models S_r \xrightarrow{SK} U_r$$

$$\text{Goal-2: } S_r \models U_r \models S_r \xrightarrow{SK} U_r$$

$$\text{Goal-3: } U_r \models S_r \xrightarrow{SK} U_r$$

$$\text{Goal-4: } U_r \models S_r \models S_r \xrightarrow{SK} U_r$$

To proceed, we convert the exchanged messages in our scheme into idealized form as given below:

$$M_2: U_r \rightarrow S_r: Aij, m_2, Auth_1: \langle Wi, ni, Tidi \rangle_{k1, k2, Y1}$$

$$M_2: S_r \rightarrow U_r: m2, Auth_2: \langle nj \rangle_{k2, Y1}$$

$$M_3: U_r \rightarrow S_r: Auth_3: \langle ni, nj' \rangle_{Tidi}$$

Besides, the understated assumptions are established for proving security of our scheme:

$$Y1: U_r \models \# ni$$

$$Y2: S_r \models \# nj$$

$$Y3: U_r \models S_r \xleftarrow{Y1} U_r$$

$$Y4: S_r \models S_r \xleftarrow{Y1'} U_r$$

$$Y5: U_r \models S_r \Rightarrow nj$$

$$Y6: S_r \models U_r \Rightarrow ni$$

Currently, the idealized forms such as M_2 , M_2 and M_3 of our scheme may be analyzed and seen in the light of stated assumptions and postulates.

Taking the first one of the idealized forms:

$$M_2: U_r \rightarrow S_r: Aij, m_2, Auth_1: \langle Wi, ni, Tidi \rangle_{k1, k2, Y1}$$

By Applying seeing postulate, we have

$$v1: S_r \triangleleft Aij, m_2, Auth_1: \langle Wi, ni, Tidi \rangle_{k1, k2, Y1}$$

According to v1, Y3 and message meaning postulate,

$$v2: S_r \models U_r \sim (Wi, ni, Tidi)$$

According to v1, Y2, freshness-conjucatenation, and nonce-verification postulates, we get

$$v3: S_r \models U_r \models (Wi, ni, Tidi)$$

The $(Wi, ni, Tidi)$ are essential parameters for mutual authentication and session key agreement.

According to Y6, v3, and Jurisdiction rule

$$v4: S_r \models (Wi, ni, Tidi)$$

Referring to Y3, v4, and session key postulate, we have

$$v5: S_r \models U_r \models S_r \xleftarrow{SK} U_r \quad \text{(Goal-2)}$$

Referring to Y6, v5, and Jurisdiction postulate

$$v6: S_r \models S_r \xleftarrow{SK} U_r \quad \text{(Goal-1)}$$

Regarding the second idealized form, we have

$$M_2: S_r \rightarrow U_r: m_2, Auth_2: \langle nj \rangle_{k2, Y1}$$

Using the seeing rule, we have

$$v7: U_r \triangleleft S_r \rightarrow U_r: m2, Auth_2: \langle nj \rangle_{k2, Y1}$$

Referring to v7, Y4 and message-meaning postulate,

$$v8: U_r \models S_r \sim (nj)$$

Regarding Y2, v8, freshness-conjucatenation, and nonce-verification postulates, we have

$$v9: U_r \models S_r \models (nj)$$

where (nj) is an essential parameter for the mutual authentication and session key establishment.

Regarding Y5, v9, and Jurisdiction postulate, we have
v10: $U_r \models (nj)$

Referring Y4, v10, and session-key postulate, we get

$$v11: U_r \models S_r \mid \equiv S_r \xleftarrow{SK} U_r \quad (\text{Goal-4})$$

Regarding Y5, v11, and Jurisdiction postulate, we have

$$v12: U_r \models S_r \xleftarrow{SK} U_r \quad (\text{Goal-3})$$

The stated BAN logic-based protocol examination establishes the fact that our model confers mutual authentication and the constructed session key (SK) is mutually established among the user U_r and server S_r .

Employing the random oracle model, we implement a formal security analysis for proving that our protocol is quite secure [29]. For the said objective, we employed the oracle *Reveal_oracle* as described below:

Reveal_oracle: This oracle would output x from the related hash digest $y=h(x)$, for sure.

The *Reveal_oracle* has been employed in Algorithm 1, $EXP1_{IBMSACP}^{HASH}$, as shown above, signifying towards the session key's disclosure if the *Reveal_oracle* is executed by inverting hash digest.

Algorithm 1. $EXP1_{IBMSACP}^{HASH}$

1. Eavesdrop the login-request $\{Aij, m_2, Auth_1\}$ where $Auth_1=h(Aij \parallel Tidi \parallel ni)$, $m_2=h(SIDj \parallel PK) \oplus ni$, and $Aij = Zi \oplus h(h(SIDj \parallel PK) \parallel ni) \oplus h(H_B(Bi) \parallel PWi) \oplus PK$.
2. Call *Reveal_oracle* oracle on the input of $Auth_1$ to get $\{Aij', Tidi, ni\}$ as $(Aij' \parallel Tidi \parallel ni) \leftarrow \text{Reveal_oracle}(Auth_1)$
3. Eavesdrop the Authentication message $\{Auth_3\}$ in verification phase, where $Auth_3=h(Tidi \parallel ni \parallel nj')$
4. Call *Reveal_oracle* on the input of $Auth_3$ to get $\{Tidi', ni, nj'\}$ as $(Tidi' \parallel ni \parallel nj') \leftarrow \text{Reveal_oracle}(Auth_3)$
5. Call *Reveal_oracle* on the input of $Tidi$ to get $\{Yi, SIDj, ni\}$ as $(Yi \parallel SIDj \parallel ni) \leftarrow \text{Reveal_oracle}(Tidi)$
6. Call *Reveal_oracle* on the input of Yi to retrieve $\{Wi, h(K \parallel b)\}$ as $(Wi \parallel h(K \parallel b)) \leftarrow \text{Reveal_oracle}(Yi)$
7. Call *Reveal_oracle* on inputting Wi to retrieve $\{Idi', K\}$ as $(Idi' \parallel K) \leftarrow \text{Reveal_oracle}(Wi)$
8. Compute session key as $SK = h(Tidi \parallel ni' \parallel nj \parallel SIDj)$
9. If $(Aij' = Aij)$ AND $(Tidi' = Tidi)$ Then
Take SK as a legitimate session key for identity (Idi') of U_i , against login request $\{Aij, m_2, Auth_1\}$

Theorem 1. *The contributed scheme is secure, if an attacker attempts to determine the mutually agreed session key (SK) among legitimate participants SP_j and U_i , provided one-way hash digest function acts nearly as a random oracle.*

Proof. In this proof [6, 8, 13-14], an adversary A , competent enough to derive the agreed session key (SK) among the participants particularly U_i and SP_j , makes a use of this *Reveal_oracle* oracle to implement $EXP1_{IBMSACP}^{HASH}$. The probability of success corresponding to $EXP1_{IBMSACP}^{HASH}$ is $Sucs1 = Prb.2[EXP1_{IBMSACP}^{HASH} = 1] - 1$. Here $Prb[E]$ depicts the event probability for an event (E). The advantage function for the above experiment can be established as $Adv_{IBMSACP}^{HASH}(tm_2, q_{Ry1}) = \max_A [Sucs1_{IBMSACP}^{HASH}]$, having execution delay time tm_2 and Reveal-query q_{Ry1} maximized on the adversary A [1]. We regard our contributed scheme as quite safe against an adversary A in recovering the agreed session key (SK) between U_i and SP_j , if $Adv_{IBMSACP}^{HASH}(tm_2, q_{Ry1}) \leq \epsilon$ for a negligibly small $\epsilon > 0$. In relation to this experiment, if the adversary is competent to invert a one-way hash digest function $h()$, it might comfortably recover the real session key (SK) shared between SP_j and U_i , and at last A wins the game. Nonetheless, in accordance with *Reveal_oracle* definition, this is polynomially unfeasible to invert hash function since $Adv_{IBMSACP}^{HASH}$ and $Adv_{IBMSACP}^{HASH}(t_1) \leq \epsilon$ for a negligibly small value, i.e. $\epsilon > 0$. Therefore, the contributed protocol may be safely considered as resistant as the security features for hash functions are tough to break in polynomial amount of time.

7. Comparison and Performance Analysis

The Chang et al. model presents a multi-server authenticated key agreement protocol and is based on light-weight symmetric key operations which are suitable for power deficient mobile devices. In this performance section, we evaluate performance efficiency of authentication protocol by Chang et al. with proposed protocol. Table 2 lists the limitations of Chang et al.'s model, while the proposed scheme acts as a vigorous authentication protocol as proven in the preceding sections. Table 2 demonstrates that Chang et al.'s model does not offer protection from stolen card threat, impersonation attack and lacks session

Table 2

Comparison for Multi-server schemes

| | Chang et al. [4] | Proposed protocol |
|----------------------------------|------------------|-------------------|
| Anonymity | ✓ | ✓ |
| Mutual authentication | ✓ | ✓ |
| Known key secrecy | ✓ | ✓ |
| Resists MiTM threat | ✓ | ✓ |
| Resists modification threat | ✓ | ✓ |
| Resists password guessing threat | ✓ | ✓ |
| Resists stolen smart card threat | × | ✓ |
| Resists impersonation threat | × | ✓ |
| Resists replay threat | ✓ | ✓ |
| Session key security | × | ✓ |

Table 3

Number of operations in Chang et al.'s model and contributed model

| | Chang et al. [4] | Ours |
|--------------------------|------------------|----------|
| Registration messages | $9 T_H$ | $8 T_H$ |
| User side | $9 T_H$ | $11 T_H$ |
| Server side | $6 T_H$ | $6 T_H$ |
| Password update messages | $4 T_H$ | $7 T_H$ |

key security, while the proposed scheme is immune to those identified threats as verified in the formal security models. The actual cost for both schemes is shown in Table 3, where different hash operations are represented with T_H , and bypassing exclusive-OR operation for its insignificant computational cost.

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Consequently, in consideration of above performance evaluation and analysis, we may infer that our protocol is more secure than Chang et al.'s protocol while bearing an equivalent cost. The proposed scheme provides immunity against impersonation and session key attacks in contrary to Chang et al.'s model. Table 3 compares the number of operations for Chang et al. protocol and contributed model and depicts that the phases of both schemes take an equivalent computational cost with a little variation in the cost of password modification phase.

8. Conclusion

The multi-server authentication serves as one of the main requirements of the current internet-based authentication framework. This manuscript studies the multi-server based Chang et al.'s remote authentication model which demonstrates that the Chang et al. scheme is prone to impersonation and session key attacks, subject to the stolen contents of smart card. The review and cryptanalysis of Chang et al.'s model has been demonstrated comprehensively. Thereafter, a proposed model is presented that foils those particular attacks with the contribution of an enhanced model. Moreover, this paper presents the formal security analysis using BAN logic and random oracle model, and evaluates the performance against the Chang et al.'s protocol.

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