REVERSIBLE LOSSLESS TRANSFORMATION FROM OWL 2 ONTOLOGIES INTO RELATIONAL DATABASES

Ernestas Vyšniauskas, Lina Nemuraitė, Rimantas Butleris, Bronius Paradauskas

Kaunas University of Technology, Department of Information Systems
Studentų St. 50-308, LT-51368 Kaunas, Lithuania
e-mail: vernest@email.lt, lina.nemuraite@ktu.lt, rimantas.butleris@ktu.lt, bronius.paradauskas@ktu.lt

Abstract. The goal of the paper is to define reversible, information preserving transformation from OWL 2 ontologies into relational databases using our proposed hybrid approach, when a part of ontology constructs is directly represented by relational database structures and another part having no direct correspondences in a relational database is stored in metadata tables. The desirable transformation is defined in QVT Relations language following additional requirements under which such transformation is reversible and does not lose semantic information when performing from ontology to database and backward.

Keywords: Ontology, relational database, OWL 2, RDB, reversible lossless transformation, QVT Relations language.

1. Introduction

Ontology comes from philosophy and defines fundamental concepts, relationships and constraints of the problem domain. Its technological embodiment, the Web Ontology Language OWL [1], now OWL 2 [2], is the indispensable means for representing human-readable and machine-processable semantics in the Semantic Web. The problem of storing large ontologies is not new and currently it attracts more and more attention. Native RDF repositories as OWLIM [3] and commercial database management systems as Oracle [4] are following the mentioned target, apart other different implementations and approaches for representing OWL ontologies using relational database constructs. Each of these approaches has its advantages and drawbacks; none of them is recognized as a standard. Recently, the W3C Consortium has announced “The Use Cases and Requirements for Mapping Relational Databases to RDF “ [5]. Naturally, all these efforts and achievements should be united for having at least a common reference and understanding how different representations could interact for reaching the vision of “Linked data” [6].

In 2006, we have proposed a hybrid approach for representing OWL ontology in relational database when a part of ontology constructs is directly represented by relational database structures, and another part is stored in metadata tables [7]. The approach was extended for OWL 2 [8]. As the quality of mapping between ontologies and database belongs on capability to perform queries, we conducted an experiment with a prototype of a tool for extracting ontologies from relational databases, satisfying our schema, and allowing the step-wise processing of SPARQL queries where SPARQL was used for querying ontology structures in a main memory and SQL was used for querying instances in the database [9]. The experiment has shown that 1) it is possible to restore the original ontology from a database created using the hybrid approach; 2) query performance times of our proposed method were better than using the memory based methods when ontology is stored using a native storage.

The limitation of our approach is the fact that ontologies undergo changes, and database structures representing ontology concepts are obliged for changing too. Metadata tables do not belong on these changes; it is an advantage of the hybrid approach. Also, the intuition tells that changes of ontology axioms represented in metadata tables are occurring much faster than changes in tables representing classes and properties of ontology. Nevertheless, the ensuring of lossless transformations in the sense of preserving information is a very important issue when ontology or database evolves.

For firming our approach, we present the specification of $\text{OWL2ToRDB}$ transformation in QVT Relation (QVT–R) language that is capable for defining bidirectional transformations. Information preserving transformations have additional requirements with regards to which we propose a reversible transformation that does not lose semantics during performing forward from ontology to database and backward.
The rest of the paper is organized as follows. In Section 2, the overview of related works is presented. Section 3 introduces OWL 2 and RDB metamodels and the overall OWL2ToRDB transformation. Section 4 analyses transformations of OWL 2 classes and class axioms; Section 5 – OWL 2 object properties, property axioms and restrictions. Section 6 summarizes the transformation of remaining OWL 2 constructs. Section 7 analyses the OWL2ToRDB transformation with regards to requirements of being a lossless transformation in the information preserving sense. Section 8 gives conclusions and highlights the future work.

2. Related Works

OWL 2, a new version of OWL, has occupied the positions of its predecessor straight after its occurrence in 2009 [2], [10]. OWL 2 offers new constructs for describing properties such as qualified cardinality restrictions; property chain axioms; local reflexivity restrictions; disjoint, reflexive, irreflexive, symmetric and anti-symmetric properties; negative property assertions; vocabulary sharing (punning) between individuals, classes, and properties; the richer set of datatypes and their restrictions etc. When extending our previous mapping, we used the same hybrid approach: direct mappings of OWL 2 class and property concepts with RDB concepts, and storing the problematic (in mapping sense) knowledge in metatables.

There are a lot of approaches for representing ontologies in databases [11]–[21] and inverse mappings from databases to ontology [22]–[26]. We can classify ontology storage models into three main cases [9]: storing ontology and its instances in the same manner (one or three tables); storing ontology concepts in database schema corresponding to full or partial ontology metamodel; and storing ontology and its instances in different schemas in order to improve access to instances while retaining the capacity of reasoning over the ontology. The first storage model does not lose information, but it uses advantages of relational databases just for saving many records, so the performance of queries to ontology information normally should be slow e.g. [14]. As an exception, the similar method is highly powered in Oracle Semantic Storage as it is supported with the native functionality of the Oracle database and optimizing techniques [4]. The second approach does not lose information, but it is oriented at storing ontologies and does not consider their relation to existing databases and advantages of database management systems [11], [15], [18], [21]. The third approach unites capabilities of ontologies and database management systems (e.g. [16], [17]). However, existing methods of that kind are losing semantics as they do not cover the sufficient subset of ontology concepts. Our proposed method intends to fill this gap by showing that it is possible to cover all ontology constructs by storing them in metadata tables, and to perform efficient querying by retaining ontology classes and properties as native RDB constructs.

There are a lot of approaches to defining transformations: the Z notation [27]; abstract syntax trees and attributes [28]; atomic and composite transformation models [29]; two-level transformations [30] etc. Every approach has its rationale, but for our work reversible, information preserving transformations are of great importance. Such transformations are vital for validation and evolution of ontology or database. First, the question about information preserving in OWL2ToRDB transformation arises as not every ontology construct may be directly mapped to a relational database. Secondly, ontologies and databases are evolving in time. Recurrent OWL2ToRDB and RDBToOWL2 transformations should not damage existing data and ensure the coherent performance.

The simplest way to ensure reversible, lossless transformations is to implement transformations in both directions and to test them. We have partially done this with our first prototype [7] and its extension [9]; now we are trying to surely verify the OWL2ToRDB transformation by defining it in a suitable, explicit transformation language. As candidate languages, ATL [31], QVT [32], formal language for model transformation specification [33], a use of predicates and functions [34], and triple graph grammars [36] were examined. The ATL is a popular but not bidirectional language; [33] presents promising, but undeveloped specification; [34] approach requires defining a lot of predicates and functions and is too cumbersome for complex transformations. Also, except QVT and triple graph grammars, all these languages are not suitable for bidirectional transformations.

The most of formal methods related to bidirectional transformations are based on graph grammars. Ehrig et al. presented a formal proof of the sufficient requirement for reversible transformations [35]. This requirement is based on the “notion of source transformation which is the projection of a triple graph transformation to its source component. It is sufficient to show that a source structure can be constructed by source transformations only”. In this case, the forward transformation is “source consistent” and it “can be inverted, i.e. there is a backward transformation leading back to the same source structure as the original one”. It means, the projection of transformation on the source model should cover all source constructs. However, this requirement is sufficient to bijective transformations only whereas most of practical transformations are not bijective, and OWL2ToRDB is so too.

The problem of defining information preserving, bidirectional and not bijective model transformations was analysed by Stevens [36]. She points that currently there is no transformation language that could guarantee the lossless transformations per se, this has to be verified. Stevens acknowledges the QVT–R language as the most suitable language for
defining bidirectional transformations and formulates the requirements for ensuring the coherent (not bijective) transformations. In Section 3, we present these criteria in more detail as they have an impact on the way transformations OWL2ToRDB are constructed.

We are considering the reversible lossless transformation as a limited bidirectional transformation that was defined by Hainaut [37]: a transformation \( T_1: M \times N \rightarrow N \) is reversible iff for all instances \( m \) of source models \( M \) exists direct transformation \( T_1 \) into instances \( n \) of target models \( N \) and also there exists a reverse transformation \( T_2: M \times N \rightarrow M \) such that \( \forall m \in M \Rightarrow T_1(m, n) = n, n \in N; \forall m \in M \Rightarrow T_2(m, T_1(m, n)) = m, n \in N. \)

Transformation \( T_1 \) is reversible, but not vice versa. That means for any arbitrary instance \( n \in N \) may not satisfy \( T_1(T_2(m, n), n) = m. \) If \( T_2 \) is reversible as well, then \( T_1 \) and \( T_2 \) are called symmetrically reversible and comprise a bidirectional lossless transformation \( T. \) Our OWL2ToRDB transformation is reversible and lossless, but not bidirectional and lossless one as the latter currently seems too big challenge because of different nature of ontologies and databases. Transforming arbitrary database into ontology is rather reverse engineering task, requiring human intervention [38]; it may be very complex taking into account procedural components such as triggers and procedures.

When defining transformations, we use the OWL 2 metamodel [2] for representing ontology. For a relational database, we use the Common Warehouse Metamodel (CWM) [39], modified by eliminating its procedural elements. Also, we have analysed the ontology definition metamodel [40], which defines the (partial) QVT R1.0 transformation between OWL1.1 and UML2.1.2.

3. The overall transformation between OWL 2 and relational metamodels

For transforming OWL 2 ontologies into database schemas, we use the original OWL 2 metamodel [2] as a source. Here we present only excerpts of that metamodel for explaining presented transformations. Figure 1 presents the top structure of OWL 2 metamodel – ontology, its annotations and axioms.

Axiom is a main instrument to define OWL 2 semantic constructs. OWL 2 building blocks are entities (i.e. classes, object properties, annotation properties, data properties, named individuals, and datatypes) that comprise the vocabulary or signature of ontology (Figure 2). One can declare an entity by stating an axiom. Conversely, annotations have no semantics but serve as a powerful means for associating additional information with ontologies, entities, and axioms.

As a target metamodel, we use a subset of CWM metamodel [39], obtained by eliminating procedural components of CWM and supplementing it with metatables (class Metatable) for preserving ontology elements having no corresponding constructs in the relational model. Also, we introduced SchemaName, TableName and ColumnName (same as a KeyName) for database schema names regarding possibly different rules for creating them (e.g. names of schemas and tables start with capital letters etc) (Figure 3).
First we present the overall transformation owl2ToRDB written in QVT Relations language [32]. For brevity, we assume that model of ontology under transformation, owl, has no importing ontology, does not import other ontologies etc. Also, we assume that all names of entities are represented as fullIRI and OWL2 classes are inserted in stead of missing domains or ranges of properties where appropriate [2]. During this transformation, ontology is transformed into RDB schema, ontology IRI is transformed into RDB schema name, metatables are created, and a row is inserted into metatable OWLOntology for preserving ontology IRI and prefix (Figure 4).

```
transformation owl2ToRDB(owl:OWL2,rdb:RDBM)
{ key Ontology{iri};
  key Entity{iri};
  key Schema{name};
  key Table{name,namespace};
  key Column{name,owner};
  key PrimaryKey{name,namespace,uniqueKey,uniqueKey:namespace};
  key OWLClasses{classId}|{className};...
  top relation OntologyToSchema
  { checkonly domain owl:ont:Ontology
    { on:OntologyToSchema
      { enforce domain rdb:schema:Schema
        { name=sn:SchemaName,
          ownedElement=classes:Metatable
          { name='OWLClasses',
            feature=mc1:Column
            { name='classId',type=Integer,
              mc2:Column{name='className',
              type=Integer},
            mc3:Column{name='superClass',
              type=Integer},
            ownedElement=fp:PrimaryKey
            { name='classId',feature=mc1,}
            uk=UniqueConstraint
            { name='subClass',}
          },
          feature=first()=mc2,
          fk=ForeignKey{name='SuperClassId',
            feature=first()=mc3},
          ont:Metatable{name='OWLOntology',
            feature=mc1:Column{name='ontologyId',
              type=Integer},
            mc2:Column{name='prefixIRI',
              type=Character},
          instance{r1:Row
            slot={s1:Slot{feature=mc1,
              value=genUniqId(mont),
              s2:Slot{feature=mc2,
              value=iri.prefix().qNameToChar()}},
          disjointClasses: Metatable{
            name='OWLDisjointClasses',
            ...},...
          }},
          when {ont.versionIRI.isEmpty();
            ont.imports.isEmpty();
            ont.directImports.isEmpty();
          }
        }
      }
    }
  }
}
```

Here we omit the lengthy definition of the remaining metatables; some of them are presented in Figures 4, 8 and 12. Operation genUniqId(table :Table):Integer generates the unique identifier for a row of a table “table”. Operation prefix(iri:IRI):Qname separates prefix from iri, where QName is a QualifiedName from XML Namespaces.

```
<owl:Ontology rdf:ID="ontIRI"
dB:PredefinedName="Definition"
OntologyID=IRIToName(iri,sn)>
  <owl:OntologyID><![CDATA[ontIRI]]></owl:OntologyID>
  <owl:OntologyID><![CDATA[prefixIRI]]></owl:OntologyID>
  <owl:OntologyID><![CDATA[versionIRI]]></owl:OntologyID>
</owl:Ontology>
```

Figure 4. Metatables for keeping information about ontologies and their IRIs
Reversible Lossless Transformation from OWL 2 Ontologies into Relational Databases

A large subset of OWL 2 axioms is transformed into rows of metatables; e.g. SubclassOf is presented later in the paper.

top relation AxiomToMetaRow { checkonly domain owl ax:Axiom{ opposite(Ontology.axioms)=ont:Ontology}; enforce domain rdb mrow:Row{ namespace.namespace=schem:Schema}; when {OntologyToSchema(ont,schem)}; where {ClassAxiomToMetaRow(ax,mrow); ObjectPropAxiomToMetaRow(ax,mrow); DataPropAxiomToMetaRow(ax,mrow)} } // AxiomToMetaRow

The important requirement for owl2ToRdb transformation being bidirectional and lossless is a possibility to convert database schema names into IRIs. It means that we should preserve a prefix when converting OWL 2 into RDB, or define a prefix if we wish to start a transformations from a database having no ontology. The transformation IRIToName itself is a simple one; however, the problem may be in defining a prefix if we wish to transform a freely chosen database schema that was not obtained by transforming some existing ontology. In such a case, we leave choosing a prefix as a decision. When transformation starts from the left side, the transformation IRIToName can be specified as operation in OCL:

context owl2ToRDB:: IRIToName(iri:IRI,sn:Character):Character post sn=let n=iri.prefix().qNameToString().size(), m=iri.iriToString().size() in sn=iri.iriToString().substring(lower=n+1,upper=m).stringToChar(),

where operations qNameToString(), iriToString(), stringToChar() (and others, as qNameToChar() used in relation OntologyToSchema) perform conversions of corresponding data types.

4. Transforming OWL 2 classes and class axioms

4.1. OWL 2 classes

In OWL 2, classes and property expressions are used to construct class expressions that represent sets of individuals by formally specifying conditions on the individual properties; individuals satisfying these conditions are instances of the corresponding class expressions. OWL 2 provides axioms that allow establishing relationships between class expressions (Figure 5).

When we are converting the OWL 2 ontology description to relational database schema, we map one ontology class to one database table.

Figure 5. The OWL 2 metamodel for class axioms [2]

As the name of an ontology class is unique in the ontology, and instances of the ontology class have unique names, we can automatically create a primary key for corresponding table and name the primary key column by adding some suffix to the class name, e.g. “Id”. Also, we create the additional column by adding “Name” suffix to the class name for saving names of instances of the class. This mapping and the example are illustrated in Figure 6.

Figure 6. Illustration of transforming OWL 2 class into RDB table

4.2. OWL 2 class axioms

The fundamental taxonomic construct for classes is the SubClassOf axiom, which allows one to state that each instance of one class expression is also an instance of another class expression. It relates the specific class to the more generic class and enables to construct the hierarchy of classes. When transforming OWL 2 ontology representation into a relational database schema, we create one table for every class in ontology with one-to-one (1:0..1) relationships between tables representing classes and their subclasses defined by the axiom subClassOf (Figure 7). Here each value of the primary key of the supertable can appear as the foreign key (and also as the primary key) for at most one row of the subtable. The subclass does not need a column for saving names of its instances, because the instance of the subclass is also the instance of the superclass and its name is saved in the superclass table.

The EquivalentClasses axiom allows one to state that several class expressions are equivalent to each other, i.e. these classes have precisely the same instances. The DisjointClasses axiom states that several class expressions are pairwise disjoint – an individual that is a member of one class cannot simultaneously be an instance of the other class. The DisjointUnion axiom allows constructing a class as a disjoint union of several class expressions.
We suggest saving this information in special metatables. All classes of the ontology are saved in OWLClasses metatable with two main columns classId, which is an automatically generated unique identification number, and className, which saves the unique name of the class (Figure 8).

Figure 8. Metaschema of OWL 2 class axioms

Also, the metatable OWLClasses has the column that is a foreign key named superClass which saves information about hierarchy of OWL classes, and the column – foreign key named annotation for relating a class with a set of its annotations. Information about groups of disjoint, disjoint union and equivalent classes is saved in metatables OWLDisjointClasses, OWLDisjointUnion and OWLEquivalentClasses (Figure 8). These tables have automatically generated unique primary keys, foreign keys from OWLClasses table and identification numbers of groups that are represented by foreign keys from metatable OWLUnitedGroups. Equivalent, disjoint and disjoint union classes have the same group identification numbers that are created during the transformation process.

OWL 2 provides a new constructHasKey which allows keys to be defined for a given class. This construct gives a list of object or data properties, which together uniquely identify named instances of a given class. For example, if individuals of the class Automobile are uniquely identified by data properties modelTitle, produceYear, and the object property isProducedBy, then the OWL 2 axiomHasKey (:Automobile :modelTitle :produceYear :isProducedBy) states that each named instance of the class Automobile is uniquely identified by this set of properties – that is, if two named instances of the class coincide on values for each of key properties, then these two individuals are the same.

For converting theHasKey axiom on some properties for the certain class to the uniqueness constraint on columns of the corresponding table, Depending on the number of HasKey properties (one or more), we create the unique key on the single column, or on a combination of columns of the table.

4.3. Defining class and class axiom transformations in QVT–R

Transformation ClassToTable transforms common features inherent for all OWL 2 classes. It generalizes transformation TopClassToTable that transforms classes having no superclass expressions. Features of classes having superclass expressions are added to the corresponding table by transformation SubClassRelationToFK. Also, the transformation ClassToTable creates a row r for each class cl in the metatable OwlClasses.

top relation ClassToTable
{ checkonly domain owl cl:Class{ entityIRI=ciri:IRI{}, opposite(Axiom.entity). opposite(Ontology.axioms)=ont:Ontology}; enforce domain rdb t:Table{ name=tn:TableName, namespace=schem:Schema, feature->{mcl:Column{ name='classId'}, value=genUniqId(mt)}; ownedElement->{pk:PrimaryKey{ name=tn+'Id', feature=select(pkcl:Column| pkcl.name=tn+'Id')}, uk:UniqueConstraint{name=tn+'Name', feature=select(tcl1:Column| tcl1.name=tn+'Name')}}; where {tn=IRIToName(ciri,tn); TopClassToTable(ci,t);}; } }/ClassToTable

Transformation of classes having no superclass expressions is further refined by the transformation TopClassToTable:

relation TopClassToTable
{ checkonly domain owl cl:Class{ entityIRI=ciri:IRI{}, opposite(Axiom.entity). opposite(Ontology.axioms)=ont:Ontology}; enforce domain rdb t:Table{ name=tn:TableName, namespace=schem:Schema, feature->{tc1:Column{ name='tn*Name', type=Character}, pk:PrimaryKey{ name='tn*Id', feature=select(pkcl:Column| pkcl.name=tn+'Id')}, uk:UniqueConstraint{name=tn*Name, feature=select(tc1:Column| tc1.name=tn*Name)}}, ownedElement->pkcl; where {tn=IRIToName(ciri,tn); TopClassToTable(ci,t);}; } }/TopClassToTable
Transformation of class cl having a superclass expression is refined by the transformation SubClassOfAxiomToFK, which creates a primary key pk for a table representing a subclass scl. This pk also is a foreign key from the table representing the corresponding superclass. Also, the name stn of the table, which represents superclass scl, is inserted into the row representing class cl in metatable OWLClasses.

top relation SubClassOfAxiomToFK{
    checkonly domain owl sub:SubClassOf{
        subclassExpression=cl:Class{
            entityIRI=cln:IRI},
        superClassExpression=scl:Class{
            entityIRI=scln:IRI},
        opposite(Ontology.axioms)=ont:Ontology};
    enforce domain rdb fk:ForeignKey{
        name=tn+'Id',
        namespace=t:Table{name=tn,
            namespace=schem:Schema},
        feature first()=fcol:Column,
        uniqueKey=pk:PrimaryKey{
            namespace=st:Table{name=stn,
                namespace=schem},
        feature first()=pcol:Column}};
    enforce domain rdb ssl:Slot{
        feature=col2:Column{name='superClass',
            value=opClassId(stn)},
        instance=mr:Row{
            classifier=mt:OWLClasses{
                namespace=schem},
        slot exists(m1|l1.feature.name='className' and l1.value=tn)};
    when {OntologyToSchema(ont,schem);
        ClassToTable(cl,t);
        ClassToTable(scl,st);
        t.feature exists(clmn|clmn.name=tn+'Id' and fcol=clmn);
        st.feature exists(sclmn|sclmn.name=stn+'Id' and pcol=sclmn);
    where {IRIToName(cln,tn);
        IRIToName(scln,stn)};}
} // SubClassOfAxiomToFK

For finding a row of a class cl in the metatable OWLClasses, the operation opClassId(cn:Character):Integer is defined that returns a value of the identifier of the row, which has the value of the column className equal to the cn, in the metatable OWLClasses:

context OWLClasses: opClassId(cn:Character): Integer
post result=self.instance select(crow:Row|
    crow.feature.name='className' and
crow.value=cn) select(isl:Slot|
    isl.feature.name='classId').value}

5. Transforming OWL 2 Object Properties, Object Property Axioms and Restrictions

5.1. OWL 2 object properties

OWL provides axioms for characterizing and establishing relationships between object property expressions.

a) ObjectProperty ≡ ForeignKey

b) ObjectProperty ≡ Table

Figure 9. Illustration of transforming OWL 2 object properties into foreign keys or tables

The object property in OWL 2 ontology relates the individual to other individuals. Depending on the cardinality of the object property (or the object property is functional or not), or existing a class with the same IRI as the object property, we transform the object property expression into the foreign key corresponding to one-to-many (1:0..*) relationship, or into the table corresponding to many-to-many (0..*:0..*) relationship between classes (Figure 9).

Metamodel of part of ObjectProperty axioms is presented in Figure 10. The ObjectPropertyDomain and ObjectPropertyRange axioms can be used to restrict the first and the second individual, connected by an object property expression, to be instances of the domain and range class expressions.

The FunctionalObjectProperty(OPE) axiom allows one to state that an object property expression OPE is functional – that is, that for each individual x, there can be at most one distinct individual y such that x is connected by OPE to y (Figure 16). This axiom is a syntactic shortcut for the axiom SubClassOf(owl:Thing ObjectMaxCardinality(1 OPE)).

So, if the OWL 2 object property is functional, or ObjectMaxCardinality or ObjectExactCardinality of the object property is ≤ 1, and the object property IRI does not match an IRI of any class in that ontology, then the foreign key corresponding to one-to-many (1:0..*) relationship between tables is created. The possibility for having a class and an object property or an individual with exactly the same IRI is a new feature of OWL 2 called “punning”. Punning allows, for example, defining properties for OWL 2 object properties by attributing these properties to a class having the same name as the object property under consideration.
If the object property is not functional, or its exact, 
min or max cardinality is > 1, or it has no cardinality 
restrictions, or if the object property IRI matches the 
IRI of some class in that ontology, then the object 
property is transformed into the table corresponding to 
many-to-many (0..*:0..*) relation between classes. In 
a case of punning, a table is needed for (1:0..*) 
relation for preserving properties of a class with 
IRI matching the object property IRI.

5.2. Object property axioms

In OWL2 there are two forms of object 
subproperty axioms. The basic form is 
SubObjectPropertyOf (OPE1 OPE2). This axiom 
states that the object property expression OPE1 is a 
subproperty of the object property expression OPE2 – 
that is, if an individual x is connected by OPE1 to an 
individual y, then x is also connected by OPE2 to y. 
E.g. in our example the class Vehicle has the object 
property hasMaker, and the class Automobile has the 
object property isProducedBy, which is the sub-
property of the property hasMaker (Figure 11). 
Information that one property is a subproperty of 
another property we save in the metatable 
OWLObjectProperties (Figure 12).

Another form of OWL2 object subproperty axiom 
is ObjectPropertyChain. The axiom SubObject 
PropertyOf (ObjectPropertyChain(OPE1... 
OPEn) OPE) states that, if an individual x is connected by a 
sequence of object property expressions OPE1, ..., 
OPEn with an individual y, then x is also connected 
with y by the object property expression OPE. E.g.
we have the class Automobile and the object property 
isVerifiedBy with the range class Assurer. The class 
Assurer has the object property employedBy with the 
range class InsuranceCompany. We can declare the 
axiom SubObjectPropertyOf (ObjectProperty 
Chain(a:isVerifiedBy a:employedBy) 
isInsuredBy) that means if some automobile is 
verified by the assurer employed by some insurance 
company, then this automobile is insured by this 
company (Figure 11).

Object property chains can be used to derive some 
additional information about relationships between 
objects. E.g. if we have both object property assertions 
isVerifiedBy and employedBy and the axiom 
SubObjectPropertyOf (ObjectPropertyChain(a:isV 
erifiedBy a: employedBy) isInsuredBy) on some 
instance, we can derive the object property assertion 
and automatically insert the appropriate value in the 
column isInsuredBy of the table Automobile during 
filling the database with instances.

ObjectPropertyChain axioms are represented in 
metatable OWLObjectPropertyChains (Figure 13). 
This table has links to the compound and component 
object properties, and the sequence number of each 
component property in the property chain.
5.3. Object property restrictions

In OWL 2 class expressions can be formed by placing restrictions on object property expressions. The ObjectSomeValuesFrom(OPE CE) class expression allows for existential quantification over an object property expression OPE, and it contains those individuals that are connected through an object property expression OPE to at least one instance of a class expression CE.

The ObjectAllValuesFrom(OPE CE) class expression allows for universal quantification over an object property expression OPE, and it contains those individuals that are connected through an object property expression OPE only to instances of a class expression CE. The ObjectHasValue(OPE a) class expression contains those individuals that are connected by an object property expression OPE to a particular individual a. Finally, the ObjectHasSelf(OPE) class expression contains those individuals that are connected by an object property expression OPE to themselves.

All semantic information about ontology constraints is saved in metatables (Figure 14). ObjectAllValuesFrom, ObjectSomeValuesFrom and ObjectHasValue restrictions have their own metatables with column restrictedObject Property, which links to the table OWLObject Properties. Metatables for ObjectAllValuesFrom and ObjectSomeValuesFrom restrictions also have a column restrictedRange Class, which points to the table of the corresponding restriction resource class. The ObjectHasValue restriction metatable has the column individualName for storing the value of the restricted resource of the corresponding property. Indication that object property has ObjectHasSelf restriction is saved in the column objectHasSelf of the OWLObjectProperties metatable.

5.4. Object property cardinality restrictions

Metamodel of object property cardinality restrictions is presented in Figure 15. The class expressions
ObjectMinCardinality, ObjectMaxCardinality, and ObjectExactCardinality contain those individuals that are connected by an object property expression to at least, at most, and exactly a given number of instances of a specified class expression, respectively. E.g. a minimum cardinality expression ObjectMinCardinality (n OPE CE) consists of a nonnegative integer n, an object property expression OPE, and a class expression CE, and contains all those individuals that are connected by OPE to at least n different individuals that are instances of CE. Similarly, the cardinality constraints ObjectMaxCardinality and ObjectExactCardinality are defined.

Cardinality restrictions of object properties are saved in the metatable OWLObjectCardinality. It has the column restrictedObjectProperty, which links to OWLObjectProperties table, and three additional nullable columns for each type of OWL cardinality restriction (Figure 14). E.g. if we have the object property with the cardinality restriction ObjectExactCardinality equal to 3, after transformation this metatable has value 3 in the field objectExactCardinality, and the other two columns objectMinCardinality and objectMaxCardinality have value “NULL”.

5.5. Object property axioms representing characteristics

The metamodel of object property axioms representing characteristics of object properties is presented in Figure 16. The InverseObjectProperty axiom can state that two object property expressions are the inverse of each other. The InverseFunctionalObjectProperty axiom states that an object property expression is inverse-functional. That is, for each individual y there can be at most one distinct individual x such that x is connected by OPE to y. The ReflexiveObjectProperty, IrreflexiveObjectProperty, SymmetricObjectProperty, AsymmetricObjectProperty, and TransitiveObjectProperty axioms allow one to state that an object property expression is reflexive, irreflexive, symmetric, asymmetric, or transitive.

OWL 2 object property axioms representing characteristics of object properties are transformed into values of columns of the rows, representing the corresponding object properties in the metatable OWLObjectProperties (Figure 13 or Figure 14).

5.6. Defining transformations of object properties, object property axioms and restrictions in QVT-R

OWL 2 functional object properties (or, equivalently, object properties having maximum cardinality value less or equal to 1; or having exact cardinality equal to 1) are transformed into foreign keys and foreign key columns of a table representing a domain class, where foreign key is defined by the primary key of the table representing a range class. The exception arises when ontology has a class C with the same IRI as the object property under consideration, e.g. OPE. Then the result of transforming OPE is merged with a table representing class C (see transformation objectPropertyToTable).

![Figure 15. Metamodel of object property cardinality restrictions](image)

![Figure 16. Metamodel of OWL 2 object property axioms defining characteristics](image)
OWL 2 object property having maximum, minimum or exact cardinality value greater than 1, or having a class with the same IRI as the object property under consideration is transformed into a table. Such transformation has 2 cases: when a class with the same IRI exists and when not. The semantics of QVT-R allows specifying these cases in one transformation because of its “check and enforce” semantics: if class exists and it is already transformed, only new features are added during the transformation execution. It means, the transformation adds new columns to the existing table.

```sql
--ObjectPropertyToTable
name='objectPropertyName',
type=Character;value=tmnn}}});

--ObjectPropertyRange
sl4:Slot{feature=col4:Column{
name='objectPropertyDomain',
type=Integer,value=mt.opClassId(dt)}};

--ObjectPropertyAxiom
sl3:Slot={feature=col3:Column{
name='objectPropertyId',
type=Integer,value=mt.owlObjectProperties}};

--ObjectExactCardinality
let exactcar:ObjectExactCardinality=
exists(fp|fp.oclIsTypeOf
(FunctionalObjectProperty))or
not op.opposite(ObjectPropertyAxiom.
objectPropertyExpression)\n\n--ObjectMaxCardinality
let maxcar:ObjectMaxCardinality=
exists(fp|fp.oclIsTypeOf
(FunctionalObjectProperty))or
not op.opposite(ObjectPropertyAxiom.
objectPropertyExpression)\n--ObjectMinCardinality
let mincar:ObjectMinCardinality=
exists(fp|fp.oclIsTypeOf
(FunctionalObjectProperty))or
not op.opposite(ObjectPropertyAxiom.
objectPropertyExpression)\n--ObjectPropertyExpression
in
exactcar.classExpression=rcl
and exactcar.cardinality=1;

--ObjectPropertyAxiom
op.opposite(ObjectPropertyAxiom.
objectPropertyExpression)\n--ObjectMaxCardinality
let maxcar:ObjectMaxCardinality=
exists(fp|fp.oclIsTypeOf
(FunctionalObjectProperty))or
not op.opposite(ObjectPropertyAxiom.
objectPropertyExpression)\n--ObjectPropertyExpression
in
maxcar.classExpression=rcl
and maxcar.cardinality=1 or
maxcar.cardinality>1 or
mincar.oclIsUndefined() or
mincar.oclIsUndefined() or
not ont.axiom.exists(ax|ax.entity.oclIsTypeOf(Class) and ax.entity.entityIRI=op.entityIRI)};

//ObjectPropertyToFK
Transformation of object property axioms in many cases results in adding column values to rows representing object property rows in metatables. E.g.

```

6. The coherence of OWL 2ToRDB transformation

As stated in [36], the coherent transformation is the one that is correct, hippocratic and undoable. The correctness of our transformation means that for every construct of OWL 2 ontology metamodel the direct and reverse transformation exist and they are related by QVT-R relations. The hippocraticness or “check then enforce” means that if transformation is not bijective, then it must look at both source and target models and do not damage them by rewriting already transformed elements. While according to Stevens [36] correctness and hippocraticness are clearly placed on QVT-R in its specification (we consider [32]) and are ensured by constructing relations, undoability also requires that any changes in source and target models could be undone. That means we should not define transformations that lead to irrevocable changes.

303
For example, changing ontology IRI into RDB schema name would become irrevocable if the operation IRIToName(iri:IRI, sn:Character): Character cannot be executed in the reverse order, i.e. a result of operation NameToIRI(sn:Character, iri:IRI):IRI is undefined (we dealt with this issue in Section 3). The same requirements were applied to all OWL2ToRDB transformations including ones defined as operations in OCL.

Let consider the correctness of the transformation OWL2ToRDB. As was mentioned in Section 0, correctness or "source consistency" means that all variety of source constructs is covered by the transformation. For meeting this requirement, first, definitions of source models should be complete though these definitions may be spread over multiple transformations; secondly, different conditions, concerning the different transformations of the same concept, may be specified in several "when" clauses.

For example, the transformation ClassToTable, presented in the paper, has two cases: TopClassToTable, when class C has no superclass, and SubclassOfAxiomToFK, when class C has a superclass. The transformation ClassToTable defines the common properties of classes and their corresponding tables (i.e. OWL2 class is transformed into RDB table, class IRI - into the identifier column of the table and a row in metatable OWLClasses with two slot values of columns representing class identifier and class name). TopClassToTable adds a column representing the class name, defines a primary key on that column, and adds a slot value "NULL" for a column superClass in the row representing that class. The transformation SubclassOfAxiomToFK adds properties to tables representing classes having superclasses; clauses “when” of these transformations involve both cases:

```
Context class inv:
  self.opposite(SubClassOf).
  superClassExpression() isNotEmpty() or
  self.opposite(SubClassOf).
  superClassExpression() notEmpty()
```

Similarly, transformations of object properties and data properties, having the class as their domain, add columns and foreign keys to the table, create rows and slot values for corresponding metatables, etc. Note that here we limit our considerations to a case when OWL2 class may have only one superclass as multiple inheritance is not permitted in well formed ontologies.

7. Conclusions

In this paper we presented the reversible and non-bijective transformations between OWL2 ontology and relational database applying hybrid mapping that combines direct representation of ontology classes, properties and instances in database tables with representing axioms and restrictions in metatables. Aiming at a lossless storing of ontologies in databases and the lossless retrieval of them into ontology reasoning tools, we presented our transformation in QVT-R language and followed the conditions under which such a transformation is coherent.

To our knowledge, reversible and lossless transformation from OWL 2 ontology into relational database was not defined for storing ontology and its instances in different schemas. Currently, we are working on the extension of our previous OWL2ToRDB implementation in two directions: 1) to implement complete reversible OWL2ToRDB transformations based on the presented QVT-R specification and 2) fulfillment of well-rounded experiments with various ontologies for comprehensively investigating and making further improvements in querying capabilities of the hybrid OWL2RDB approach.

References


Reversible Lossless Transformation from OWL 2 Ontologies into Relational Databases


Received March 2011.